

### Understanding the Electrostatic Equations

The electrostatic equation chart is capable of solving almost every electrostatic problem, if you understand it well.

**SCALARS** →  $q_1$  causes  $F$  at a point a distance  $r$  from  $q_2$ .  $q_1$  is a  $2^{\text{nd}}$  charge at point  $P$ .

<b>Potential</b> $V = k_c \frac{q_1}{r}$ $\Delta V = -E\Delta d$ $(g \text{ [J/kg]})$ $(g \text{ [N/kg]})$ $E = k_c \frac{q_1}{r^2}$ $= \frac{V}{\Delta d}$ <b>Force</b>	<b>Potential Energy:</b> $PE = k_c \frac{q_1 q_2}{r}$ $\Delta PE = -qE\Delta d$ $(mgh \text{ [J]})$ $(mg \text{ [N]})$ $F_e = k_c \frac{q_1 q_2}{r^2}$ $= qE$ <b>Force</b>
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For multiple charges ( $\times d$ )  
 $E$  is different for each charge, so you must  $\times$  or  $\div$  by  $r$  for each individual charge (ie:  $PE_{\text{total}} \neq F_{\text{total}}$ )

**VECTORS** →  $\times q_1$

$q_1$  is independent of the charges which cause  $E$ .  
 So, for multiple charges, you can  $\times$  or  $\div$   $F_{\text{net}}$  by  $q_2$ .

**k<sub>c</sub> Equations**

Around point charges there is a non-uniform electric field. Notice that  $E$  has different strength and direction at points A and B. Therefore, you will have to use the  $k_c$  equations.

Calculating  $V$  at point A is simple, since  $V$  is a scalar:  
 $V = k_c \frac{q_1}{r_1} + k_c \frac{q_2}{r_2}$  where  $r_1$  is the distance to  $q_1$ , etc.

Calculating  $F$  or  $PE$  would only be possible, of course, if there was a third charge at point A. Then:  
 $F_{\text{net},3} = k_c \frac{q_1 q_3}{r_1^2} + k_c \frac{q_2 q_3}{r_2^2}$  and vector addition would be necessary to find  $F_{\text{net}}$ .

Fill in the following blanks with the words **electrons** or **protons**.

\_\_\_\_\_ are negatively charged and \_\_\_\_\_ are positively charged. The \_\_\_\_\_ reside in the nucleus of atoms and are tightly bound; they will never leave an atom as a result of electrostatic procedures. On the other hand, \_\_\_\_\_ are located outside the nucleus and are easily removed from or added to atoms. As an object begins to gain or lose \_\_\_\_\_ from its atoms, it becomes positively or negatively charged. A negatively charged object has more \_\_\_\_\_ than \_\_\_\_\_ . A positively charged object has more \_\_\_\_\_ than \_\_\_\_\_ .

Use the triboelectric series to answer the following questions:  
 When you pull a **cotton** sweater off your **skin**, electrons are transferred from the \_\_\_\_\_ (cotton, skin) to the \_\_\_\_\_ (cotton, skin). As a result, your body acquires a \_\_\_\_\_ (+, -, ) charge and the cotton sweater acquires a \_\_\_\_\_ (+, -, ) charge.

When you rub a **glass** rod with a **silk** cloth, electrons are transferred from the \_\_\_\_\_ (glass, silk) to the \_\_\_\_\_ (glass, silk). As a result, the glass rod acquires a \_\_\_\_\_ (+, -, ) charge and the silk cloth acquires a \_\_\_\_\_ (+, -, ) charge.

Suppose you rub a rubber rod with a silk cloth and a second rubber rod with a wool sweater. The silk cloth will acquire a \_\_\_\_\_ (+, -, ) charge; the wool sweater will acquire a \_\_\_\_\_ (+, -, ) charge. The sweater and the cloth will then be observed to \_\_\_\_\_ (attract, repel, not interact with) each other.

Suppose you rub a glass rod with a silk cloth and a second glass rod with rabbit fur. The silk cloth will acquire a \_\_\_\_\_ (+, -, ) charge; the rabbit fur will acquire a \_\_\_\_\_ (+, -, ) charge. The rabbit fur and the silk cloth will then be observed to \_\_\_\_\_ (attract, repel, not interact with) each other.

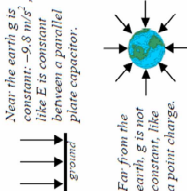
### A Gravity Analogy

**E is like g**  
 The acceleration due to gravity, "g", is also known as the gravitational field. g is caused by mass (the earth). E is caused by charges, q.

**F<sub>e</sub> is like mg**  
 $F_e = mgh$ , which is the weight due to a mass put inside a constant g. Likewise, q feels a force from the E created by q<sub>1</sub> (or the capacitor), so  $F_e = -qE$ .

**PE is like mgh**  
 $PE = mgh = -qE\Delta d$ . Remember that PE equals the work to move the object to that place and PE equals the amount of kinetic energy the object will have if released.

**V (-ED) is like gh**  
 Think of gh as the gravitational potential for energy at a point (in J/kg). The gravitational potential for energy could be increased by increasing h or g (on Jupiter, for instance).



Far from the earth, g is not constant, like a point charge.

Near the earth, g is constant, -9.8 m/s<sup>2</sup>, like E is constant between a parallel plate capacitor.

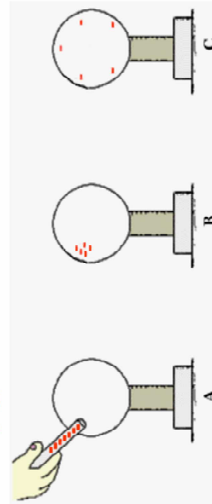
Both m's have the same force of weight when g is constant. F<sub>e</sub> is position independent, too, if E is constant (lines are !).

At B, F<sub>e</sub> = 0, but PE ≠ 0 because it would take PE to get it there. C doubles the PE given by A, since if released B feels 2 × q's pushing it away.

The 4 kg has more PE than the 2 kg, but then have the same potential (gh). The 2 kg has more potential than the 5 kg.

<b>Constant Field—</b> (Field lines are parallel, like near the earth, or near a charged flat plate)		<b>Point Sources (2 particles)</b> Field lines radiate outward	
Gravitational (caused by mass) $= mg$ (in N) $= g$ (in N/kg) $= mg\Delta h$ (in J) $h=0$ on ground $= g\Delta h$ (in J/kg)	Electric (caused by charge) $= qE$ (in N) $= \frac{V}{\Delta d}$ (in N/C) $\Delta PE = -qE\Delta d$ (in J) $\Delta V = -E\Delta d$ (in J/C)	Gravitational (caused by mass) $F_g = G \frac{m_1 m_2}{r^2}$ (in N) $= G \frac{q_1}{r^2}$ (in N/kg) $PE = G \frac{m_1 m_2}{r}$ (in J) $= G \frac{m_1}{r}$ (in J/kg)	Electric (caused by charge) $F_e = k_c \frac{q_1 q_2}{r^2}$ (in N) $E = k_c \frac{q_1}{r^2}$ (in N/C) $PE = k_c \frac{q_1 q_2}{r}$ (in J) $V = k_c \frac{q_1}{r}$ (in J/C)
Field (potential for a force)	Potential Energy (PE or U)	Potential (for energy) or Voltage	

Consider the conduction charging process described below:



- A. A teacher holds a negatively charged metal bar by its insulating handle and touches it to a metal sphere (attached to an insulating stand).
- B. The teacher pulls the metal bar away and the metal sphere acquires a charge.
- C. The excess negative charge spreads uniformly about the surface of the metal sphere.

### Triboelectric Series

- Celluloid
- Sulfur
- Rubber
- Copper, Brass
- Amber
- Wood
- Cotton
- Human Skin
- Silk
- Cat Fur
- Wool
- Glass
- Rabbit Fur

3. Diagram A is the charging step. How does the sphere become charged?
  - a. Electrons move from the insulating stand into the sphere.
  - b. Electrons move from the charged metal bar into the sphere.
  - c. Protons move from the sphere into the negatively charged bar.
4. When the metal bar is pulled away in Diagram B, the metal bar is \_\_\_\_\_  
 a. positively charged  
 b. electrically neutral  
 c. still negatively charged, but has fewer excess electrons than it previously did.
5. Diagram C shows the excess negative charge distributed differently than it is in Diagram B. Explain why the excess negative charge would distribute itself as it does in Diagram C.

**Alteration in both the Quantity of Charge and the Distance**

Two charged objects have a repulsive force of .080 N. If the charge of one of the objects is doubled, and the distance separating the objects is doubled, then what is the new force?

Two charged objects have a repulsive force of .080 N. If the charge of both of the objects is doubled and the distance separating the objects is doubled, then what is the new force?

Two charged objects have an attractive force of .080 N. If the charge of one of the objects is increased by a factor of four, and the distance separating the objects is doubled, then what is the new force?

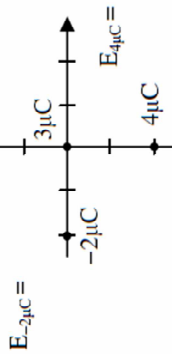
Two charged objects have an attractive force of .080 N. If the charge of one of the objects is tripled and the distance separating the objects is tripled, then what is the new force?

Use your understanding of electric force and electric field to fill in the following table.

Charge creating the E field (C)	Charge used to test the E field (C)	Force experienced by test charge (N)	Electric Field Intensity (N/C)	Distance (fictional units)
a. $4.0 \times 10^{-4} \text{ C}$	$1.0 \times 10^{-6} \text{ C}$	0.20 N		d
b. $4.0 \times 10^{-4} \text{ C}$	$2.0 \times 10^{-6} \text{ C}$	0.40 N	$2.0 \times 10^5 \text{ N/C}$	d
c. $8.0 \times 10^{-4} \text{ C}$	$1.0 \times 10^{-6} \text{ C}$	0.40 N	$4.0 \times 10^5 \text{ N/C}$	d
d. $8.0 \times 10^{-4} \text{ C}$	$2.0 \times 10^{-6} \text{ C}$	0.60 N		d
e. $8.0 \times 10^{-4} \text{ C}$		0.10 N		2d
f. $8.0 \times 10^{-4} \text{ C}$	$1.0 \times 10^{-6} \text{ C}$		$1.0 \times 10^5 \text{ N/C}$	2d
g. $8.0 \times 10^{-4} \text{ C}$	$2.0 \times 10^{-6} \text{ C}$			2d
h. $8.0 \times 10^{-4} \text{ C}$		0.10 N		2d
i. $4.0 \times 10^{-4} \text{ C}$			$8.0 \times 10^5 \text{ N/C}$	0.5 d
j. $4.0 \times 10^{-4} \text{ C}$				0.5 d

Two fixed charges are placed on the x-y axis, as shown on the diagram. A third charge of  $3\mu\text{C}$  is moved from infinity to the origin. Each line is 1 cm.

A. Calculate the electric field due to each charge at the origin.



B. Calculate the net electric field at the origin, both magnitude and direction.

C. Calculate the net force on the  $3\mu\text{C}$  charge.

A balloon with a charge of  $4.0 \times 10^{-5} \text{ C}$  is held a distance of 0.10 m from a second balloon having the same charge. Calculate the magnitude of the repulsive force. **PSYW**

Calculate the electrical force (in Newtons) exerted between a 22-gram balloon with a charge of  $-2.6 \mu\text{C}$  and a wool sweater with a charge of  $+3.8 \mu\text{C}$ ; the separation distance is 0.75 m. (NOTE: a  $\mu\text{C}$  or microCoulomb is a unit of charge;  $10^6 \mu\text{C} = 1 \text{ C}$ ) **PSYW**

**Types of Charging**  
Charging means gaining or losing electrons. Matters can be charged with three ways, charging by friction, charging by contact and charging by induction.

**Charging by Friction**  
When you rub one material to another, they are charged by friction. Material losing electron is positively charged and material gaining electron is negatively charged. Amount of gained and lost electron is equal to each other.

**Charging by Contact**  
There are equal numbers of electrons and protons in a neutral matter. If something changes this balance we can say it is charged.  
1. When charged object touches to a neutral object, they both have same charge.  
2. When two charged matter touch each other, total charge of the system is conserved and they share the total charge according to their capacities. If they have same amount of different charges, when we touch one another they become neutral. If the amount of charges is different then, either flow of charge they are both negatively or positively charged. Having opposite charges after contact is impossible.

**Charging by Induction**  
A and B conductors are neutral at the beginning. When we put a positively charged plate near them, it attracts the electrons in the conductors. Electrons move to the left part and protons stays. Thus, when we separate plates A and B they are charged by induction. A is negatively charged and B is positively charged. Be careful, there is no contact; they are charged only by induction.

5. A  $+3\text{C}$  charge is moved in a uniform electric field that has a field strength of  $500 \text{ N/C}$ .

A. Calculate the distance it moves parallel to the field.



B. Which direction does the electric field point?



C. Calculate the  $\Delta\text{PE}$  of the charge.



D. Since electric field is also in  $\text{V/m}$  and the plates are separated by 18mm, calculate the voltage of the plates.

E. If this is a  $6\mu\text{F}$  capacitor, how much charge is held on it?