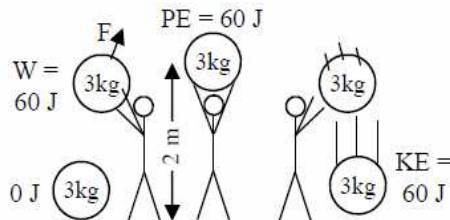


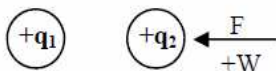
Remember that potential energy (PE) is energy of position. **PE equals the work that moved the object and also equals the kinetic energy it will have after it is released.**



Electric Potential Energy for Two Charges

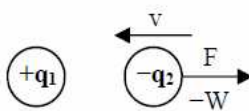
Electric Potential Energy (in J) $\rightarrow PE = k_c \frac{q_1 q_2}{r}$

When q_2 is brought from infinity to a point a distance of "r" meters from q_1 .



q_2 has PE due to its position near q_1 . When like charges are brought together from infinity, +W is necessary, increasing q_2 's PE, like compressing a spring.

If opposite charges are brought together, a force (and -W) is necessary to hold them back. PE is negative because the force is reducing the PE it had at infinity. At infinity it could have accelerated all the way to the positive charge, but now it can only accelerate a short distance. **Anytime a charge moves the direction it wants to move, it loses PE.**



Ex: A $-2\mu\text{C}$ charge is 3 mm from a $6\mu\text{C}$ charge. Calculate the electric potential energy.

Variables:

$k_c = 9 \times 10^9$
 $q_1 = -2 \times 10^{-6} \text{C}$
 $q_2 = 6 \times 10^{-6} \text{C}$
 $r = 3 \times 10^{-3} \text{m}$

$$PE = k_c \frac{q_1 q_2}{r}$$

$$= 9 \times 10^9 \frac{(-2 \times 10^{-6})(6 \times 10^{-6})}{(3 \times 10^{-3})}$$

$$= 9 \times 10^9 \frac{-1.2 \times 10^{-11}}{3 \times 10^{-3}} = -36 \text{ J}$$

And for unlike charges PE is -.

Only Δ PE Matters

With gravitational potential energy we usually assume that the zero point (the reference point) is at the ground. **For two charges our reference point is infinity—where the electric force is zero.** In a uniform electric field, there is no zero point, so only the change of PE is important.

Δ PE in a Uniform Electric Field

Change of Electric Potential Energy (in J) $\rightarrow \Delta PE = -Eqd$

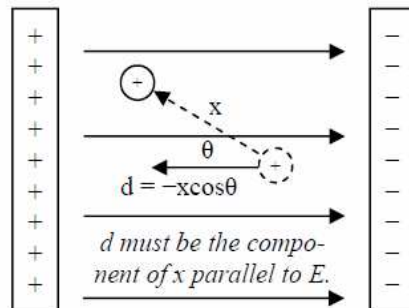
Electric Charge (in C) \rightarrow
 Electric Field (in N/C) \rightarrow
 Distance Moved Parallel to E (in m) \rightarrow

$PE = F_e r$ OR $\Delta PE = F_e d_{\parallel}$

F_w (weight) = mg and $PE = mgh$, so $PE = (F_w)h$. Likewise: if you know F_e , then $PE_{\text{electric}} = (F_e)d$. Simply multiply F_e by the distance moved or the distance between the charges:

If $F_e = k_c \frac{q_1 q_2}{r^2}$ then, $PE = \left(k_c \frac{q_1 q_2}{r^2} \right) r = k_c \frac{q_1 q_2}{r}$

The electric field is uniform within charged parallel plates. E always points from + to -. As always, up or and right are +.



Ex: A $5.6\mu\text{C}$ charge is moved 1.2mm to the left in a constant 2.3 N/C electric field. If the positive plate is on the left, what is the change of potential energy of the charge?

Variables:

$q = 5.6 \times 10^{-6} \text{C}$
 $d = -1.2 \times 10^{-3} \text{m}$
 (left is negative)
 $E = 2.3 \text{ N/C}$
 (+ on left means E points right)

$$\Delta PE = -Eqd$$

$$= -2.3(5.6 \times 10^{-6})(-1.2 \times 10^{-3})$$

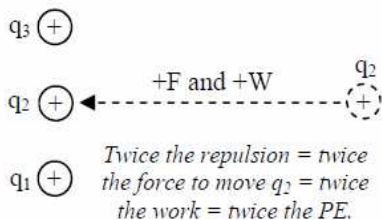
$$= 1.55 \times 10^{-8} \text{ J}$$

And we know that the positive sign is correct because when a + charge moves closer to the + plate, it gains energy.

PE is a scalar

If there are multiple charges, just add the potential energies together. Vector addition is unnecessary.

At q_2 's position the electric field (E) and electric force (F) are both zero. As vectors the E and F from q_1 and q_3 balance each other. Yet, as a scalar, PE is not zero. There is twice as much PE as with only one charge.



PE is not zero because it would take work to bring q_2 to this point. With two positive charges repelling, it takes twice as much force (and work) to push q_2 here, storing twice as much energy. Though it requires no force to keep it at the midpoint, the slightest bump would cause q_2 to fly off, until all of its PE becomes kinetic energy at infinity.

